Statistics Unit 1: Exploring Data: Describing patterns and departures from patterns	TIME FRAME:	10 weeks
ATIONAL COMMON CORE STANDARDS:	MATHEMATICAL PRAC	CTICES:
 derstand and evaluate random processes underlying statistical experiments \$-IC.1 Understand statistics as a process for making inferences about population parameters based on a random sample from that population. scon quantifatively and use units to solve problems N-Q.2 Define appropriate quantities for the purpose of descriptive modeling. N-Q.1 Use units as a way to understand problems and to guide the solution of multi-step problems: choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. N-Q.3 Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. mmarize, represent, and interpret data on a single count or measurement variable \$-ID.1 Represent data with plots on the real number line (dot plots, histograms, and box plots). \$-ID.2 Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets. accounting for possible effects of extreme data points (outliers). eate equations that describe numbers or relationships A -CED.4 Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. mmarize, represent, and interpret data on a single count or measurement variable \$-ID.4 Use the mean and standard deviation of a data set to fit it a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets, and tables to estimate areas under the normal curve. terpretinear models \$-ID.4 Be the mean and standard deviation of a scatter plot, and describe how the variables are related. \$-ID.4 Be there force or enclation and causation. mmarize, tepresent, and interpret data on two categoric	 others. 4. Model with m 5. Use appropriation strategically. 6. Attend to pre 7. Look for and restructure. 8. Look for and restructure. 8. Look for and restructure. 	colving them. actly and ble arguments he reasoning of athematics. ate tools cision. make use of express regularity

 approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational absolute value, exponential, and logarithmic functions. Interpret functions that arise in applications in terms of the context F-IF.4 For a function that models a relationship between two quantities, interpret key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity. F-IF.5 Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. F-IF.6 Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. Construct and compare linear, quadratic, and exponential models and solve problems F-LE.1 Distinguish between situations that can be modeled with linear functions and with exponential functions. F-LE.1b Recognize situations in which one quantity changes at a constant rate per unit interval relative to another. Interpret the structure of expressions A-SSE.1 Interpret expressions that represent a quantity in terms of its context. A-SSE.1b Interpret complicated expressions by viewing one or more of their parts as a single entity. 	F
ESSENTIAL QUESTIONS	ASSESSMENT
ESSENIIAL QUESTIONS	
 What is data? How do we understand and communicate data? Can you lie with statistics? How and to what extent? What assumptions can be made from data? How can graphical displays be manipulated to present misleading information? How can data analysis be used to predict future happenings? Does the data always lead to the truth? How does one assess normality? Why is the normal distribution essential to the study of statistics? How does the normal distribution apply to the real world? 	Formative: • At the bell activities • Question and answer • Homework • Quizzes • Constructed response/open- ended problem solving • Performance tasks • Sample AP Essays Summative: • Performance based assessments • Quizzes • Tests • Constructed response/ open- ended problem solving • Performance tasks • Project

		 Released Practice AP Exam Death Penalty Project Statistics Caloric content of hot dogs and a comparison of meat Linear Regression Project
	PA COMMON CORE STANDARDS	Keystone Eligible Content
S	 CC.2.1.HS.F.1: Apply and extend the properties of exponents to solve problems with rational exponents. CC.2.1.HS.F.3: Apply quantitative reasoning to choose and interpret units and scales in formulas, graphs, and data displays. CC.2.1.HS.F.4: Use units as a way to understand problems and to guide the solution of multi-step problems. CC.2.1.HS.F.5: Choose a level of accuracy appropriate to limitations on measurement when 	A1.1.2 Linear Equations A1.1.2.1 Write, solve, and/or graph linear equations using various methods. A1.1.2.2.2
UNIT OF INSTRUCTION: PATTERNS AND DEPARTURES FROM PATTERNS	 CC.2.1.HS.F.5: Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. CC.2.2.HS.D.1: Interpret the structure of expressions to represent a quantity in terms of its context. CC.2.2.HS.D.2: Write expressions in equivalent forms to solve problems. CC.2.2.HS.C.2: Graph and analyze functions and use their properties to make connections between the different representations. CC.2.2.HS.C.6: Interpret functions in terms of the situations they model. CC.2.4.HS.B.1: Summarize, represent, and interpret data on a single count or measurement variable. CC.2.4.HS.B.2: Summarize, represent, and interpret data on two categorical and quantitative variables. CC.2.4.HS.B.3: Analyze linear models to make interpretations between quantities. CC.2.8.C.2: Use concepts of functions to model relationships between quantities. 	 Interpret solutions to problems in the context of the problem situation. A1.1.3.1.2 Identify or graph the solution set to a linear inequality on a number line. A1.2.1.1.1 Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically.
	CC.2.1.7.D.1: Analyze proportional relationships and use them to model and solve real-world and mathematical problems.Essential Skills and Understanding	 A1.2.2.2.1 Draw, identify, find, and/or write an equation for a line of best fit for a scatter plot. A1.2.3.2.2
DESCRIBING	 Choose an appropriate display for categorical data. Be able to create an appropriate display for categorical data and clearly describe the reasoning for the choice. Be able to read and interpret displays of conditional distributions of one variable for more. Be able to identify an appropriate display for quantitative data and clearly justify the choice. Be able to construct a display for quantitative data. Know how to compare the distributions of groups by comparing their shape, center, and spread. 	 Analyze data; make predictions, and/or answer questions based on displayed data (box-and whisker plots, stem-and-leaf plots, scatter plots, measures of central tendency, or other representations). A1.2.3.2.3 Make predictions using the

Understand the impact of outliers in the data.	equations or graphs of best-fit
 Use a graphing calculator to construct a basic histogram. 	lines of scatter plots.
 Understand the standard deviation tells how the data surrounds the mean. 	
Use a graphing calculator to find a 5-number summary of a variable and create a	
boxplot.	
 Understand which numerical descriptions resist outliers and which do not. 	
Know how to clearly describe numerical summaries in written form.	
Be able to use the Normal model to estimate observations falling within certain standard	
deviations of the mean.	
Know how to find the percentage.	
Recognize patterns in a scatter plot.	
Know how to describe a given scatter plot in detail.	
 Draw conclusions about the value of the correlation coefficient be able to defend the 	
strength of the value.	
Be able to distinguish between correlation and causation.	
Be able to distinguish between correlation and association.	
Know how to create a scatter plot by hand and with technology.	

	DIFFERENTIATION ACTIVITIES: Teacher directed differentiated instructional projects and activities are ongoing and based on student need.				
ENRICHMENT:	 The Practice of Statistics: Third Edition online resources Studylsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks 		 Khan Academy Prentice Hall Algebra 2 The Practice of Statistics: Third Edition online resources Studylsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks 		
RESOURCES:	 MiniTab Statistics Software Microsoft Excel PDE SAS portal: <u>http://www.pdesas.org</u> Graphing calculator Khan Academy <u>www.studyisland.com</u> The Practice of Statistics: Third Edition 2008 Daniel Yates, David Mo Stats: Modeling the World 2007 Bock, Velleman, De Veaux Statistics in Practice: Second Edition 1998 Blaisdell CollegeBoard.com Practice Released AP Exam materials 	ore, Do	aren Starnes		

AP Statistics UNIT 2: Sampling and Experimentation: Planning and	TIME FRAME: 6 weeks		
Gr. 11,12 conducting a study	IIME FRAME. 8 WEEKS		
 NATIONAL COMMON CORE STANDARDS: Make inferences and justify conclusions from sample surveys, experiments, and observational studies S-IC.3 Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each. S-IC.4 Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling. S-IC.6 Evaluate reports based on data. S-IC.5 Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant. Understand and evaluate random processes underlying statistical experiments S-IC.1 Understand statistics as a process for making inferences about population. S-IC.2 Decide if a specified model is consistent with results from a given data-generating process, e.g., using simulation. 	 MATHEMATICAL PRACTICES: Make sense of problems and persevere in solving them. Reason abstractly and quantitatively. Construct viable arguments and critique the reasoning of others. Model with mathematics. Use appropriate tools strategically. Attend to precision. Look for and make use of structure. Look for and express regularity in repeated reasoning. 		
ESSENTIAL QUESTIONS	ASSESSMENT		
 How do we obtain data? Why is it important? What is bias? How can it be identified? How can it be prevented? To what extent is data biased? To what extent can data be purposely biased? To what extent does data collection methodology affect results? Does size matter? 	Formative: • At the bell activities • Question and answer • Homework • Quizzes • Constructed response/open-ended problem solving • Performance tasks • Sample AP Essays Summative: • Performance based assessments • Quizzes • Tests • Constructed response/open-ended problem solving • Performance based assessments • Quizzes • Tests • Constructed response/open-ended problem solving • Performance tasks • Project • Released Practice AP Exam		

PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
 PA COMMON CORE STANDARDS CC.2.1.HS.F.5: Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. CC.2.4.HS.B.2: Summarize, represent, and interpret data on two categorical and quantitative variables. CC.2.4.HS.B.4: Recognize and evaluate random processes underlying statistical experiments. CC.2.4.HS.B.5: Make inferences and justify conclusions based on sample surveys, experiments, and observational studies. Essential Skills and Understanding Be able to identify the population in sampling. Be able to identify the population in sampling. Be able to identify bias. Know how to use a calculator to select a simple random sample. Recognize the difference between an observation study and an experiment. Be able to identify bias. Identify all elements of an experiment. Design a randomized experiment. Explain in writing why a randomized comparative experiment can give good evidence for cause and effect relationships. 	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES M07.D-S.1. Use random sampling to draw inference about a population. M07.D-S.1.11 • Determine whether a sample is a random sample given a real-world situation. M07.D-S.1.12 • Use data from a random sample to draw inferences about a population with an unknown characteristic of interest.

	DIFFERENTIATION ACTIVITIES: Teacher directed differentiated instructional projects and activities are ongoing and based on student need.				
ENRICHMENT:	 The Practice of Statistics: Third Edition online resources StudyIsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks 	REMEDIATION:	 Khan Academy Prentice Hall Algebra 2 The Practice of Statistics: Third Edition online resources StudyIsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks 		
RESOURCES:	 MiniTab Statistics Software Microsoft Excel PDE SAS portal: http://www.pdesas.org Graphing calculator Khan Academy www.studyisland.com The Practice of Statistics: Third Edition 2008 Daniel Yates, David Mo Stats: Modeling the World 2007 Bock, Velleman, De Veaux Statistics in Practice: Second Edition 1998 Blaisdell CollegeBoard.com Practice Released AP Exam materials Resource Requirements: The school ensures that each student has a college-level statistics The school ensures that each student has access to a graphing content of the school provides access to a computer to aid in investigating content.	textbo	bok for individual use, inside and outside of the classroom. For with statistical capabilities.		

AP Statistics Unit 3:	Anticipating Patterns: Exploring Random Phenomena Using Probability and Simulation	TIME FRAME:	10 weeks
 S-MD.1 Define value to each distribution us S-MD.2 Calcu the probabilit S-MD.3 Devel space in whice S-MD.4 Devel space in whice S-MD.4 Devel space in whice S-MD.5 Weigh values and fir S-MD.5a Find Make inferences and studies S-IC.4 Use data develop a me Use probability to evelop studies S-MD.7 Analy testing, media S-MD.5 (+) We payoff values 	values and use them to solve problems e a random variable for a quantity of interest by assigning a numerical n event in a sample space; graph the corresponding probability ing the same graphical displays as for data distributions. late the expected value of a random variable; interpret it as the mean of	in solving th 2. Reason abs 3. Construct v critique the 4. Model with 5. Use approp 6. Attend to p 7. Look for an	e of problems and persevere hem. stractly and quantitatively. riable arguments and reasoning of others. mathematics. priate tools strategically. orecision. d make use of structure. d express regularity in

ESSENTIAL QUESTIONS	ASSESSMENT
 ESSENTIAL QUESTIONS What is the probability of understanding probability? When is probability a sure thing? How can we base decisions on chance? How can probability be used to simulate events and to predict future happenings? What are the benefits of simulating events as opposed to gathering real data? What is randomness? How can modeling predict the future? To what extent does our world exhibit binomial and geometric phenomena? When is probability a sure thing? How can we base decisions on chance? How can modeling predict the future? To what extent does our world exhibit binomial and geometric phenomena? How can we base decisions on chance? How can modeling predict the future? To what extent does our world exhibit binomial and geometric phenomena? How can we base decisions on chance? Boos the central limit Theorem to understand the variability of a statistic? Does the Central Limit Theorem test one's limit? 	ASSESSMENT Formative: Journals/logs • KWL chart KWL chart • At the bell activities Question and answer • Individual white boards/Promethean Board ActiVotes Board ActiVotes • Homework Quizzes • Constructed response/open-ended problem solving Performance tasks • Exit slips Summative: • CDT's Performance based assessments • Quizzes Tests • CDT's Performance tasks • Tests Ocnstructed response/open-ended • Performance based assessments Performance tasks • Tests Performance tasks • Tests Performance tasks • Project Performance tasks

	PA COMMON CORE STANDARDS	Keystone Eligible Content
⊲	CC.2.1.HS.F.5: Choose a level of accuracy appropriate to limitations on measurement	A1.2.3 Data Analysis
: MENA	when reporting quantities.	
S:	CC.2.2.HS.D.1: Interpret the structure of expressions to represent a quantity in terms of its	A1.2.3.3 Apply probability to practical
х ол	context.	situations.
	CC.2.4.7.B.3: Investigate chance processes and develop, use, and evaluate probability	
PATTERNS: M PHENOM	models.	A1.2.3.3.1
L	CC.2.4.6.B.1: Demonstrate an understanding of statistical variability by displaying,	Find probabilities for compound events
žğ	analyzing, and summarizing distributions.	(e.g., find probability of red and blue,
ANTICIPATING	CC.2.4.HS.B.6: Use the concepts of independence and conditional probability to	find probability of red or blue) and
	interpret data.	represent as a fraction, decimal, or
ĔŽ	CC.2.4.HS.B.7: Apply the rules of probability to compute probabilities of compound	percent.
AN DR	events in a uniform probability model.	
PLC		A2.2.1 Patterns, Relations, and Functions
EXP	Essential Skills and Understanding	
		A2.2.1.1 Analyze and/or use patterns or
	 Be able to explain independent and dependent variables. 	relations.

Calculate the mean and variance of a discrete random variable. ٠ Use technology or the formula to calculate binomial and geometric ٠ probabilities. • Construct cumulative distribution tables and histograms. Understand that dependency of variability on size of sample. Be able to demonstrate a sampling distribution by simulation. ٠

A2.2.1.1.1

• Analyze a set of data for the existence of a pattern, and represent the pattern with a rule algebraically and/or graphically.

A2.2.3 Data Analysis

A2.2.3.2 Apply probability to practical situations

A2.2.3.2.1

• Use combinations, permutations, and the fundamental counting principle to solve problems involving probability.

A2.2.3.2.2

• Use odds to find probability and/or use probability to find odds.

A2.2.3.2.3

• Use probability for independent, dependent, or compound events to predict outcomes.

ENRICHMENT:	 Teacher directed differentiated instructional projects and activities are ongoing MiniTab Statistics Software Pearson - Stats: Modeling the World Pearson - Elementary Statistics Microsoft Excel The Practice of Statistics: Third Edition online resources StudyIsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks 	REMEDIATION:	 Khan Academy Prentice Hall Algebra 2 The Practice of Statistics: Third Edition online resources Studylsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks
RESOURCES:	 MiniTab Statistics Software Microsoft Excel PDE SAS portal: <u>http://www.pdesas.org</u> Graphing calculator Exit Tickets Khan Academy <u>www.studyisland.com</u> The Practice of Statistics: Third Edition 2008 Daniel Yates, David Moore, Daren Starr Stats: Modeling the World 2007 Bock, Velleman, De Veaux Statistics in Practice: Second Edition 1998 Blaisdell 	nes	

AP Statistics Unit 4: Gr. 11,12	Statistical Inference: Estimating Population Parameters and Testing Hypotheses	TIME FRAME:	10 weeks
 S-IC.4 Use data fr margin of error th S-IC.6 Evaluate re S-IC.5 Use data fr decide if differen Summarize, represent, ar S-ID.5 Summarize relative frequenc relative frequenc Understand independent S-CP.4 Construct associated with e 	RE STANDARDS: http://conclusions.from.sample.surveys, experiments, and observational studies om a sample survey to estimate a population mean or proportion; develop a rough the use of simulation models for random sampling. eports based on data. om a randomized experiment to compare two treatments; use simulations to ces between parameters are significant. ht interpret data on two categorical and quantitative variables categorical data for two categories in two-way frequency tables. Interpret ies in the context of the data (including joint, marginal, and conditional ies). Recognize possible associations and trends in the data. cc and conditional probability and use them to interpret data and interpret two-way frequency tables of data when two categories are be ach object being classified. Use the two-way table as a sample space to are independent and to approximate conditional probabilities.	 persevere in 2. Reason abstrative 3. Construct vicritique the 4. Model with the 5. Use appropriative 6. Attend to prime 7. Look for an extractories 	of problems and solving them. ractly and ly. able arguments and reasoning of others. mathematics. iate tools ecision. I make use of
	ESSENTIAL QUESTIONS	ASSES	SMENT
 Is it reasonable to How is statistical i How is probability How can decision To what extent sh What does it mea How do you dete What does it mea How does one dis How can we test How can we verif How does one dis How do you find o How does one dis How does one dis How does one dis How can we test How does one dis How can we test 	nce do you need before you are able to make a reasonable conjecture? think that different people require different amounts of convincing? Inference used to draw conclusions from data? To used to express the strength of our conclusions? In so be based on chance? ould decisions be made based on chance? In to be 95% confident when speaking to statistical reports? In to be 95% confident when speaking to statistical reports? In to make an inference? In to make an inference? It inguish among the various confidence intervals? a series of proportions? If that two variables are independent? Critical values for a chi-square test? In the various tests of significance? It inguish among the various tests of significance? It is solve of a correlation? It is solve of a correlation? model to make statistical inference?	ended prob Performance Sample AP E <u>Summative:</u> Performance Quizzes Tests Constructed ended prob Performance Project	d answer I response/open- Iem solving e tasks Essays e based assessments I response/open- Iem solving

 CC.2.1.HS.F.S: Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. CC.2.4.HS.B.S: Moke inferences and justify conclusions based on sample surveys, experiments, and observational studies. CC.2.4.HS.B.S: Moke inferences about populations based on random sampling concepts. CC.2.4.F.B.1: Draw inferences about populations based on random sampling concepts. CC.2.4.F.B.2: Draw informal comparative inferences about two populations. Essential Skills and Understanding Understand that dependency of variability on size of sample. Be able to draw conclusions about the distribution of the mean by using the sampling distribution model. Be able to interpret a sampling distribution model and describe it. Explain what is meant by 95% confidence. Calculate a confidence interval for the mean of a normal population. Recognize when the confidence interval formula cannot be used. Find appropriate sample size at o obtain a confidence interval of specified margin of error. Determine what Type I and Type II errors are in the context of a situation. Understand the connection between sample size and power. Explain the meaning for the p-value. Calculate the zstatistic and p-value for one-sided and two-sided tests. Recognize when you can use the z test. Determine statistical significance. Be able to state the null and alternative hypothesis for testing the difference between two proportions. Know how to determine when making inference about the difference between two exactly intervention the intervention of the mean the difference between two exactly encound the intervention of the mean the difference between two exactly accurate the rule and the rational the intervention of the mean of a situation.
 Know how to determine when making inference about the difference between two population proportions would be invalid. Know how to find a confidence interval for the difference between two Proportions. Understand that failing to reject the null hypothesis does not mean accepting it.

UNIT OF INSTRUCTION:

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